

# 國立彰化師範大學 99 學年度碩士班招生考試試題

系所：機電工程學系

組別：乙組(選考乙)

科目：電磁學

☆☆請在答案紙上作答☆☆

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- Given an electric field  $\mathbf{E} = \mathbf{a}_x(y - c_1 z) + \mathbf{a}_y(c_2 x - 4z) - \mathbf{a}_z(2c_3 y + z)$ 
  - Determine the coefficients  $c_1$ ,  $c_2$ , and  $c_3$  if  $\mathbf{E}$  is irrotational. (8%)
  - Determine the electric potential  $V$ . (7%)
- Please derive the boundary conditions for the electrostatic field at an interface between two media. (15%)
- A point charge  $q$  is located at a distance  $D$  from the center of a grounded conducting sphere of radius  $r$  ( $r < D$ ). Determine
  - the charge distribution induced on the surface of the sphere. (10%)
  - the total charge induced on the sphere. (10%)
- Lightning strikes a lossy dielectric sphere which has  $\epsilon = 1.1\epsilon_0$ ,  $\sigma = 10 \text{ S/m}$ , radius = 0.1 m at time  $t = 0$ , depositing uniformly in the sphere with a total charge 1 mC.
  - Determine the electric field intensity both inside and outside of the sphere. (10%)
  - Calculate the time it takes for the charge density in the sphere to diminish to 1% of its initial value. (10%)
- A current  $I$  flows in the inner conductor of an infinitely long coaxial line and returns via the outer conductor. The radius of the inner conductor is  $a$ , and the inner and outer radii of the outer conductor are  $b$  and  $c$ , respectively. Find the magnetic flux density  $\mathbf{B}$  for all regions and plot  $|\mathbf{B}|$  versus  $r$ . (15%)
- A circular loop of  $N$  turns of conducting wire lies in the  $xy$ -plane with its center at the origin of a magnetic field specified by  $B = a_z B_0 \sin(5\pi r^2 / 3b) \cos \omega t$ , where  $b$  is the radius of the loop and  $\omega$  is the angular frequency.
  - Find the emf induced in the loop. (10%)
  - What is the phase relationship between the induced emf and the magnetic field? (5%)