## 國立彰化師範大學99學年度碩士班招生考試試題

系所:電機工程學系

科目:工程數學

☆☆請在答案紙上作答☆☆ (寫出過程)

共2頁,第1頁

I. (20%) Find the general solutions of the following differential equations.

(a) 
$$y''+4y'+4y = xe^x$$
 (10%)

(b) 
$$x^3y'''+3x^2y''-2xy'+2y=0$$
 (10%)

II. (10%) Use Laplace transform to solve the differential equation.

$$y''+2y'+y=2\cos t$$
,  $y(0)=3$ ,  $y'(0)=0$ 

III. (10%) Solve the following integral equation.

$$y(t) = t + \int_{0}^{t} \sin(t - \tau) y(\tau) \cdot d\tau$$

IV. (10%) Find the Fourier series of a periodic function defined as

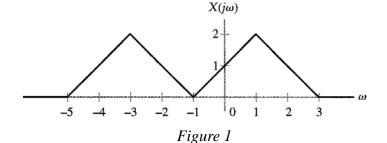
$$f(t) = \begin{cases} 0, & -\frac{\pi}{\omega} < t \le 0 \\ 2\sin(\omega t), & 0 < t \le \frac{\pi}{\omega} \end{cases}, \quad f(t + \frac{2\pi}{\omega}) = f(t).$$

V. (10%) The Fourier transform of x(t) is shown in *Figure 1*. Please find the following quantities

without explicitly computing x(t).

(a) 
$$x(0)$$
 (5%)

(b) 
$$\int_{-\infty}^{\infty} x(t)dt \quad (5\%)$$



VI. (20%) Evaluate the following integrals by means of the residue theorem

(a) 
$$\oint_C \frac{e^{2z}}{(z-i)^2} dz$$
,  $C: |z| = 2$  (5%)

(b) 
$$\oint_C \frac{\sin z}{(z-\pi)^3} dz$$
,  $C: |z| = 2$  (5%)

(c) 
$$\frac{1}{2\pi i} \oint_C \frac{1}{z(z^6 - 1)(z + 3)} dz$$
,  $C: |z| = 2$  (10%)

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共2頁,第2頁

VII. (10%) If  $\vec{F} = (2y + z)\vec{a}_x + (y - 2)\vec{a}_y + (3y - x)\vec{a}_z$ , evaluate the integral  $\iint_S \vec{F} \cdot d\vec{s}$  over the closed surface of the cube bounded by  $0 \le x \le 1$ ,  $0 \le y \le 1$ ,  $0 \le z \le 1$ .

VIII.(10%) If  $\vec{A} = 3\vec{a}_{\rho} + 2\vec{a}_{\phi} + 5\vec{a}_{z}$  and  $\vec{B} = -2\vec{a}_{\rho} + 3\vec{a}_{\phi} - \vec{a}_{z}$  are given at points P(3, 30°, 5) and

Q(4, 60°, 3), respectively, find  $\vec{C} = \vec{A} + \vec{B}$  at point S(2, 45°, 4) expressed in cylindrical coordinates.