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共6頁,第1頁

I. Multiple Choices Question (40%)

- 1. In constructing confidence interval estimate for the difference between two population proportions, we :
 - (A) pool the population proportions when the populations are normally distributed
 - (B) pool the population proportions when the population means are equal
 - (C) pool the population proportions when they are equal
 - (D) never pool the population proportions
- 2. For testing the difference between two population proportions, the pooled proportion estimate should be used to compute the value of the test statistic when the :
 - (A) populations are normally distributed
 - (B) sample sizes are small
 - (C) samples are independently drawn from the populations
 - (D) null hypothesis states that the two population proportions are equal

3. In testing the null hypothesis $H_0: p_1 - p_2 = 0$, if H_0 is false, the test could lead to :

- (A) a Type I error
- (B) a Type II error
- (C) either a Type I or a Type II error
- (D) None of the above
- 4. The number of degrees of freedom associated with the *t* test, when the data are gathered from a matched pairs experiment with 10 pairs, is :
 - (A) 10
 - (B) 20
 - (C) 9
 - (D) 18
- 5. The president of a state university collected data from students concerning building a new library, and classified the responses into different categories (strongly agree, agree, undecided, disagree, strongly disagree) and according to whether the student was male or female. To determine whether the data provide sufficient evidence to indicate that the responses depend upon gender, the most appropriate test is :
 - (A) chi-squared goodness-of-fit test
 - (B) chi-squared test of a contingency table (test of independence)
 - (C) chi-squared test of normality
 - (D) chi-squared test for comparing five proportions

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- 6. The Spearman rank correlation coefficient must be used to determine if a relationship exits between two variables when :
 - (A) one of the variables may be ordinal
 - (B) Both of the variables may be ordinal
 - (C) Both variables are interval and the normality requirement may not be satisfied.
 - (D) All of the above statements are correct.
- 7. When the necessary conditions are met, a two-tail test is being conducted to test the difference between two population proportions. If the value of the test statistic z is 2.05, then the p-value is :
 - (A) 0.4798
 - (B) 0.0404
 - (C) 0.2399
 - (D) 0.0202
- 8. The regression line $\hat{y} = 3 + 2x$ has been fitted to the data points (4,8), (2,5), and (1,2). The sum of the squared residuals will be :
 - (A) 7
 - (B) 15
 - (C) 8
 - (D) 22
- 9. Which of the following statements is not true?
 - (A) Multicollinearity exists in virtually all multiple regression models.
 - (B) Multicollinearity is also called collinearity and intercorrelation.
 - (C) Multicollinearity is a condition that exists when the independent variables are highly correlated with the dependent variable.
 - (D) Multicollinearity does not affect the F-test of the analysis of variance.
- 10. In an ANOVA test, the test statistic is F = 6.75. The rejection region is F > 3.97 for the 5% level of significance, F > 5.29 for the 2.5% level, and F > 7.46 for the 1% level. For this test, the *p*-value is
 - (A) greater than 0.05
 - (B) between 0.025 and 0.05
 - (C) between 0.01 and 0.025
 - (D) approximately 0.05

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II. Short Answers (60%)

- 1. A plant produces sulfur bricks that are used for structure in high-stress industrial environments. The production process is currently molding bricks with a mean weight of μ =1.740 kilograms and a standard deviation of σ =0.03 kilograms. (10%)
 - (a) For a random sample of 50 bricks, find the probability that the sample mean will exceed 1.745.
 - (b) For a random sample of 50 bricks, find the probability that the sample mean will lie within ± 0.005 of μ .
- 2. If X_1 , X_2 , X_3 are three normally and independently distributed random variables with mean 7, 28, 6 and variances 4, 12, 4, respectively. Suppose $Y=2X_1+X_2+3X_3$ (10%)
 - (a) Find the distribution of Y and its parameters.
 - (b) If a random sample of size 150 taken from the distribution of Y, find the probability of sample mean lies between 59 and 61.
- 3. The life of a certain type of device has an advertised failure rate of 0.01 per hour. The failure rate is constant and the exponential distribution applies. (15%)
 - (a) What is the probability that 200 hours will pass before a failure is observed?
 - (b) What is the probability that a failure is observed between 100 and 200 hours?
 - (c) What is the mean time that elapses between failures?
- 4. In order to test the hypotheses

$$H_0: \mu_1 - \mu_2 = 0$$

 $H_1: \mu_1 - \mu_2 \neq 0,$

we independently draw a random sample of 18 observations from a normal population with standard deviation of 15, and another random sample of 12 from a second normal population with standard deviation of 25. If we set the level of significance at 10%, determine the power of the test when $\mu_1 - \mu_2 = 5$ (10%)

5. A partial ANOVA table in a randomized block design is shown below :

Source of Variation	SS	$d\!f$	MS	F
Treatments	*	4	*	*
Blocks	3,120	6	*	*
Error	*	*	115	
Total	12,600	34		

(a) Fill in the missing values (identified by asterisks) in the above ANOVA Table. (7%)

(b) Can we infer at the 5% significance level that the treatment means differ? (4%)

(c) Can we infer at the 5% significance level that the block means differ? (4%)

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Standard Normal Cumulative Probability Table

Cumulative probabilities for NEGATIVE z-values are shown in the following table:

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-3.4	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0002
-3.3	0.0005	0.0005	0.0005	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0003
-3.2	0.0007	0.0007	0.0006	0.0006	0.0006	0.0006	0.0006	0.0005	0.0005	0.0005
-3.1	0.0010	0.0009	0.0009	0.0009	0.0008	0.0008	0.0008	0.0008	0.0007	0.0007
-3.0	0.0013	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
10	0.0007	0.0004	0.0074	0.0000	0.0000	0.0056	0.0050	0.0044	0.0000	0.0000
-1.9	0.0287	0.0261	0.0274	0.0208	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.0	0.0359	0.0351	0.0344	0.0330	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0440	0.0430	0.0427	0.0410	0.0409	0.0401	0.0392	0.0304	0.0375	0.0307
-1.0	0.0668	0.0007	0.0520	0.0510	0.0618	0.0495	0.0400	0.0473	0.0403	0.0455
-1.7	0.0000	0.0000	0.0045	0.0000	0.0010	0.0000	0.0004	0.0002	0.0071	0.0000
-1.4	0 0808	0 0793	0 0778	0 0764	0 0749	0 0735	0.0721	0 0708	0 0694	0.0681
-1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
-1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
-0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
-0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
-0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
-0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

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F Values for $\alpha = 0.05$

					d_1				
d_2	1	2	3	4	5	6	7	8	9
1	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	240.5
2	18.51	19.00	19.16	19.25	19.3	19.33	19.35	19.37	19.38
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28
26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04
120	3.92	3.07	2.68	2.45	2.29	2.17	2.09	2.02	1.96
inf	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88

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選考丙 科目:_

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t-Distribution Table



The shaded area is equal to α for $t = t_{\alpha}$.

df	t.100	t.050	t.025	t.010	t.005
1	3.078	6.314	12.706	31.821	63.657
2	1.886	2.920	4.303	6.965	9.925
3	1.638	2.353	3.182	4.541	5.841
4	1.533	2.132	2.776	3.747	4.604
5	1.476	2.015	2.571	3.365	4.032
6	1.440	1.943	2.447	3.143	3.707
7	1.415	1.895	2.365	2.998	3.499
8	1.397	1.860	2.306	2.896	3.355
9	1.383	1.833	2.262	2.821	3.250
10	1.372	1.812	2.228	2.764	3.169
11	1.363	1.796	2.201	2.718	3.106
12	1.356	1.782	2.179	2.681	3.055
13	1.350	1.771	2.160	2.650	3.012
14	1.345	1.761	2.145	2.624	2.977
15	1.341	1.753	2.131	2.602	2.947
16	1.337	1.746	2.120	2.583	2.921
17	1.333	1.740	2.110	2.567	2.898
18	1.330	1.734	2.101	2.552	2.878
19	1.328	1.729	2.093	2.539	2.861
20	1.325	1.725	2.086	2.528	2.845
21	1.323	1.721	2.080	2.518	2.831
22	1.321	1.717	2.074	2.508	2.819
23	1.319	1.714	2.069	2.500	2.807
24	1.318	1.711	2.064	2.492	2.797
25	1.316	1.708	2.060	2.485	2.787
26	1.315	1.706	2.056	2.479	2.779
27	1.314	1.703	2.052	2.473	2.771
28	1.313	1.701	2.048	2.467	2.763
29	1.311	1.699	2.045	2.462	2.756
30	1.310	1.697	2.042	2.457	2.750
32	1.309	1.694	2.037	2.449	2.738
34	1.307	1.691	2.032	2.441	2.728
36	1.306	1.688	2.028	2.434	2.719
38	1.304	1.686	2.024	2.429	2.712
∞	1.282	1.645	1.960	2.326	2.576