

國立彰化師範大學 102 學年度碩士班招生考試試題

系所：統計資訊研究所

科目：微積分

☆☆請在答案紙上作答☆☆

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1. Evaluate the indefinite integral $\int \frac{1}{(x^2+3x+1)^2} dx$. (15%)
2. Find $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{\sqrt{n^2+kn+3k^2}}{n^2}$. (15%)
3. Find the radius of convergence and interval of convergence of the series $\sum_{n=1}^{\infty} (-1)^n \frac{(x+3)^n}{n3^n}$. (20%)
4. Find the derivative of the function F defined by $F(x) = \int_x^{x^2+7} \exp(3t^2) dt$. (10%)
5. Evaluate the integral $\int_{-\infty}^{\infty} \exp(-x^2) dx$. (20%)
6. Find the minimum of $f(x) = \cos x + |x|$ on the real line. (20%)