# 國立彰化師範大學101學年度碩士班招生考試試題

### 系所: <u>電信工程學研究所</u>

### 科目: \_ 電磁學

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## ☆☆請在答案卷上作答☆☆

#### Weighting: Each problem counts 20%

- 1. For a scalar function f and a vector function  $\overline{A}$ , prove that  $\nabla \times (f\overline{A}) = f \nabla \times \overline{A} + (\nabla f) \times \overline{A}$  in Rectangular coordinates system and calculate  $\nabla(1/\rho) \nabla \times (\cos \theta \nabla \phi)$  in appropriate coordinates systems. (show all your work)
- 2. Given a static electric field intensity  $\overline{E} = a_x kx^2 + a_y ky$  (V/m) in free space, find the charge density distribution  $\rho_y$  at the point (3, 4, 0) (cm). (please show all your work)
- 3. Find the capacitance of the parallel-plate capacitor shown in Figure. Find the electric field intensity between the plates if a potential  $V_o$  is applied to the top plate and the bottom plate is grounded. Also find the surface charge density on each plate conductor (top and bottom plates). (20%)



4. Find the magnetic flux density at point *P* in Fig. 1. where *P* is the center of the circle and the current *I* follows from the  $-\infty$  and goes around the circle of radius *b* clockwise, and then follows to  $+\infty$ .



Fig. 1 The wire current I follows from  $-\infty$  and goes around a circle of a radius b, then to  $+\infty$ .

5. A uniform plane wave in air with  $\overline{E}_i(x,t) = \stackrel{\wedge \wedge}{a_x} E_o \cos(10^8 t - \beta z) + a_y E_o \sin(10^8 t - \beta z)$  (V/m) is incident normally on a perfect conducting wall in the z = 0 plane. Find the following in phasor form (a) Calculate the value of  $\beta$ 

- (b)  $E_r$  and  $H_r$  (reflected fields)
- (c) Determine the polarization of the incident wave and the reflected wave. (LP, RHCP, LHCP, or EP)
- (d) Find the induced current density on the wall