## 國立彰化師範大學九十六學年度碩士班招生考試試題

**系所:電信工程學研究所** 

## 科目:電磁學

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☆☆請在答案紙上作答☆☆

## Weighting: Each problem counts 20%

- 1. For a scalar function f and a vector function  $\overline{A}$ , prove that  $\nabla \times (f \overline{A}) = f \nabla \times \overline{A} + (\nabla f) \times \overline{A}$  and  $\nabla \cdot (f \overline{A}) = f \nabla \cdot \overline{A} + \overline{A} \cdot \nabla f$  in Rectangular coordinates system.
- 2. Given a static electric field intensity  $\overline{E} = \hat{a}_x kx + \hat{a}_y ky + \hat{a}_z kz$  (mV/m) in free space, find the charge density distribution  $\rho_y$  at the point (3, 4, 0) (cm). (please show all your work)
- 3. Find the capacitance of the parallel-plate capacitor shown in Figure. Find the electric field intensity between the plates if a potential  $V_0$  is applied to the top plate and the bottom plate is grounded. Also find the surface charge density on each plate conductor.



4. A uniform plane wave in air with  $\overline{E}_i(x,t) = \hat{a}_x E_o \sin(2\pi \times 10^8 t - \beta z) (V/m)$  is incident normally

on a perfect conducting wall in the z = 0 plane. Find the following in phasor form

- (a)  $\overline{E}_r$  and  $\overline{H}_r$  (reflected fields)
- (b) The induced current density on the wall
- 5. Find the expression of the input impedance,  $Z_{in}$ , for a cascaded transmission line shown in figure. If  $R_L$  is a pure real value and the  $\lambda$  is the guided wavelength of the wave propagated in the transmission line, find the values of  $R_t$  and  $l_t$  for the matching condition (no reflection). Calculate the  $Z_{in}$  under the match condition.

